

# Adaptive Impedance Controller for Human-Robot Arbitration based on Cooperative Differential Game Theory

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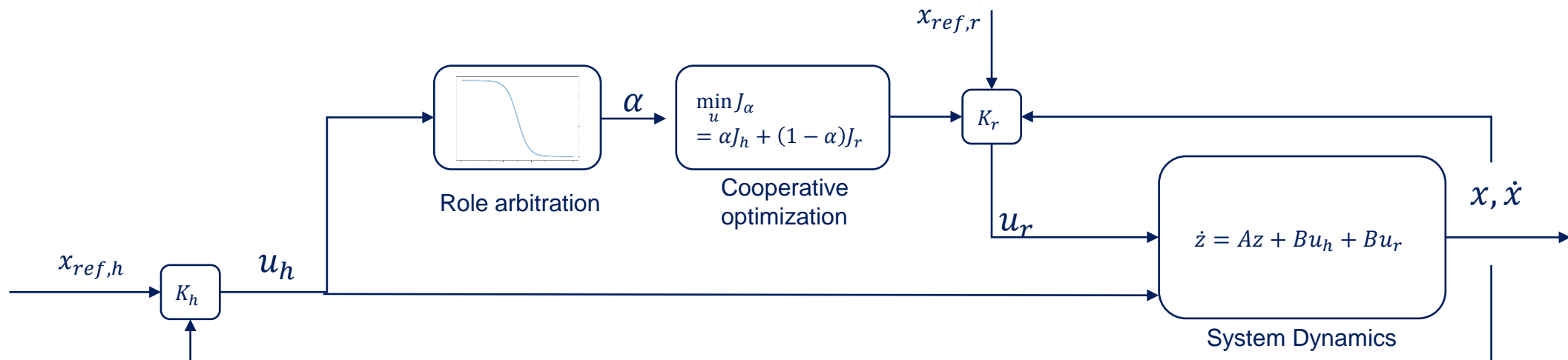
# Motivation and goal

**Motivation:** Humans and robots have complementary capabilities that should be combined to improve both working conditions and quality of results

**Goal:** develop a methodology that allows shared autonomy and role arbitration between a human and a robot

# Method

Cooperative Differential Game: Pareto optima are usually better than Nash equilibria, naturally allowing “agreement” between players



# Method

$$\dot{x} = Ax + B_h u_h + B_r u_r$$

System dynamics

Remark: linear model for the human are useful approximation of the more complex human behavior

$$J_h = \int_0^{\infty} \{x^T Q_h x + u_h^T R_h u_h\} dt$$

Human cost function

$$J_r = \int_0^{\infty} \{x^T Q_r x + u_r^T R_r u_r\} dt$$

Robot cost function

$$J(\alpha) = \alpha J_h + (1 - \alpha) J_r = \int_0^{\infty} \{x^T Q(\alpha) x + u^T R(\alpha) u\} dt$$

Cooperative cost function

$\alpha$ : weighting factor. Selects the solution among the ones lying on the Pareto frontiers. The choice of  $\alpha$  is the so-called Bargaining Theory

# Method

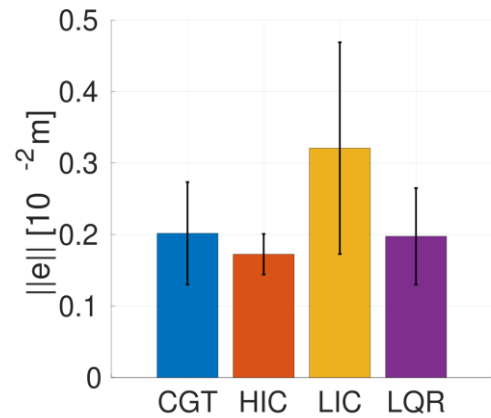
- **Role Arbitration:** the mechanism that assigns control of the task to either the human or the robot
- **Bargaining solution:** the parameter  $\alpha$  is made variable according to the human will to lead the action
- **Results:** a Variable Impedance controller, which varies stiffness and damping parameters due to the adaptation of the robot's role of leader/follower according to human intentions.

# Experiments

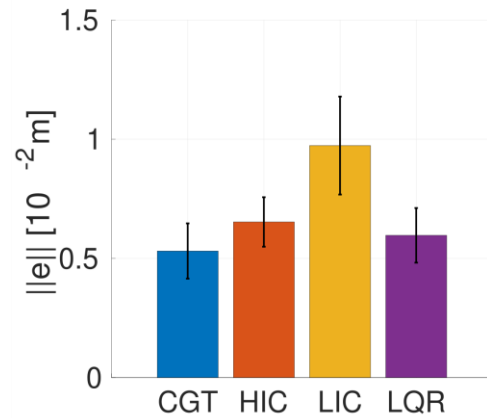
Human and robot have to follow two partially overlapping trajectories. The robot does not know the human trajectory. When the human applies a force, the robot behaves as a follower, otherwise as leader



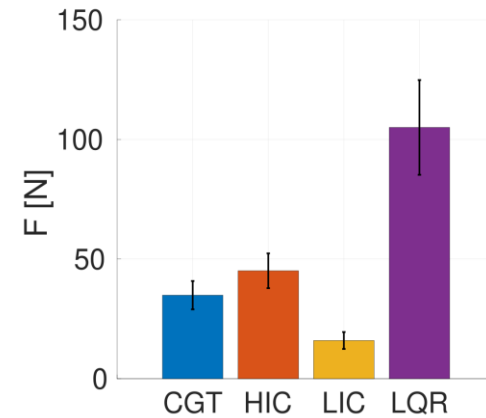
# Results



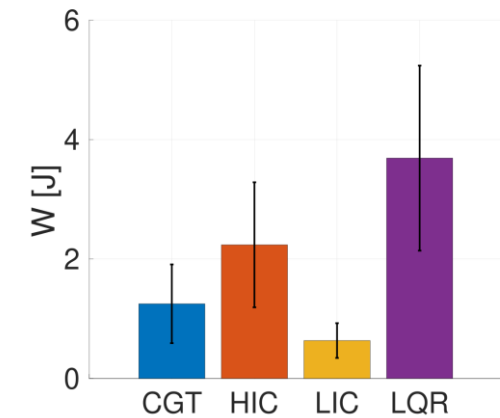
Path tracking error



Trajectory trac error

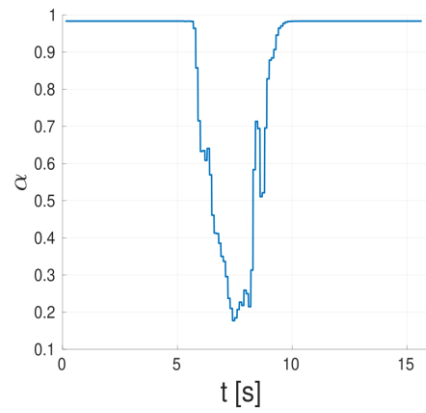


Exchanged force

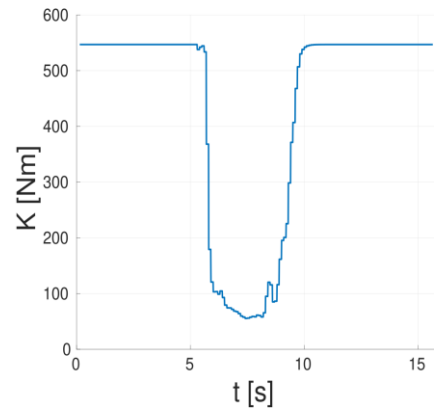


Mechanical work

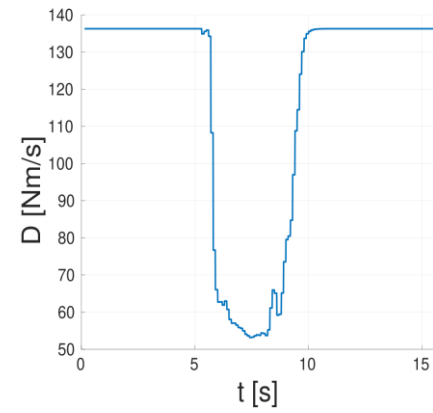
# Results



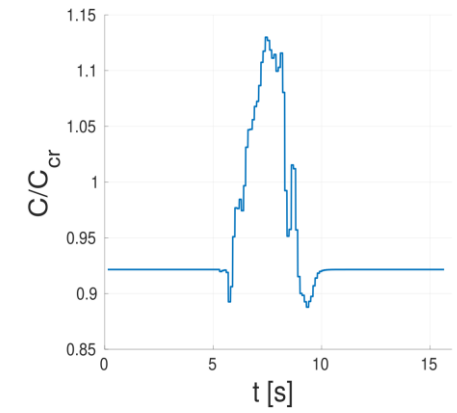
$\alpha$



Variable stiffness



Variable damping



Variable critical damping



# Thank you for your attention



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